

# *Mastering Uncertainty:* Optimizing Real-Time Systems for Robustness and Resilience

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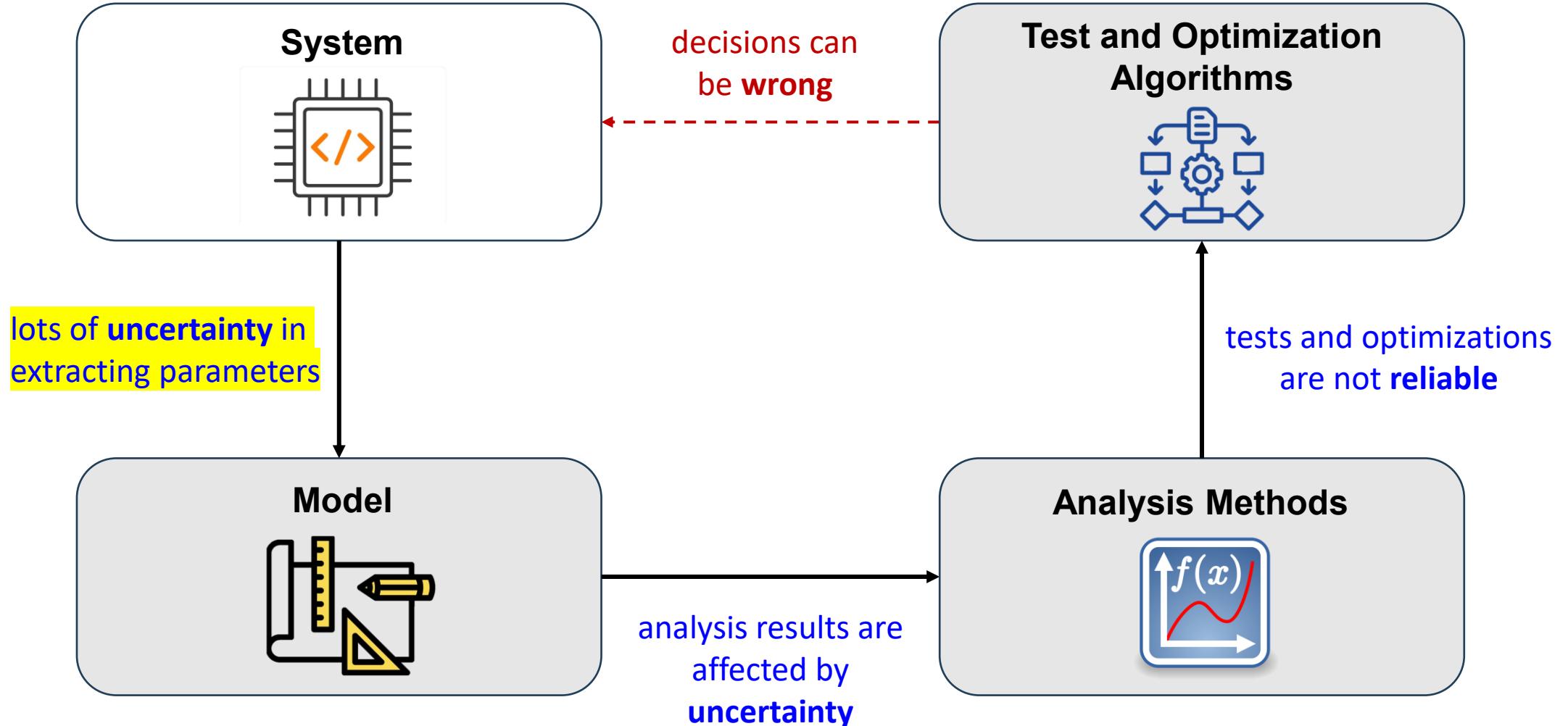
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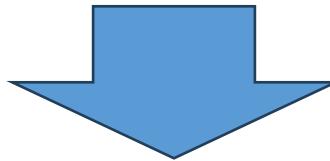


# Design & Test Loop



# The Elephant in The Room

- **Let's accept the reality:** In many systems WCETs are unknown
  - They're the same ones we use to motivate most of today's research on real-time systems
  - Response-time bounds cannot be trusted
  - There's a major source of **uncertainty** in our models



## Design for uncertainty

- What's the best configuration to **maximize robustness** in the face of uncertainty?
- How to make a system as **resilient** as possible given uncertainty?
- How **risky** is a system under uncertainty?

# Modeling Uncertainty

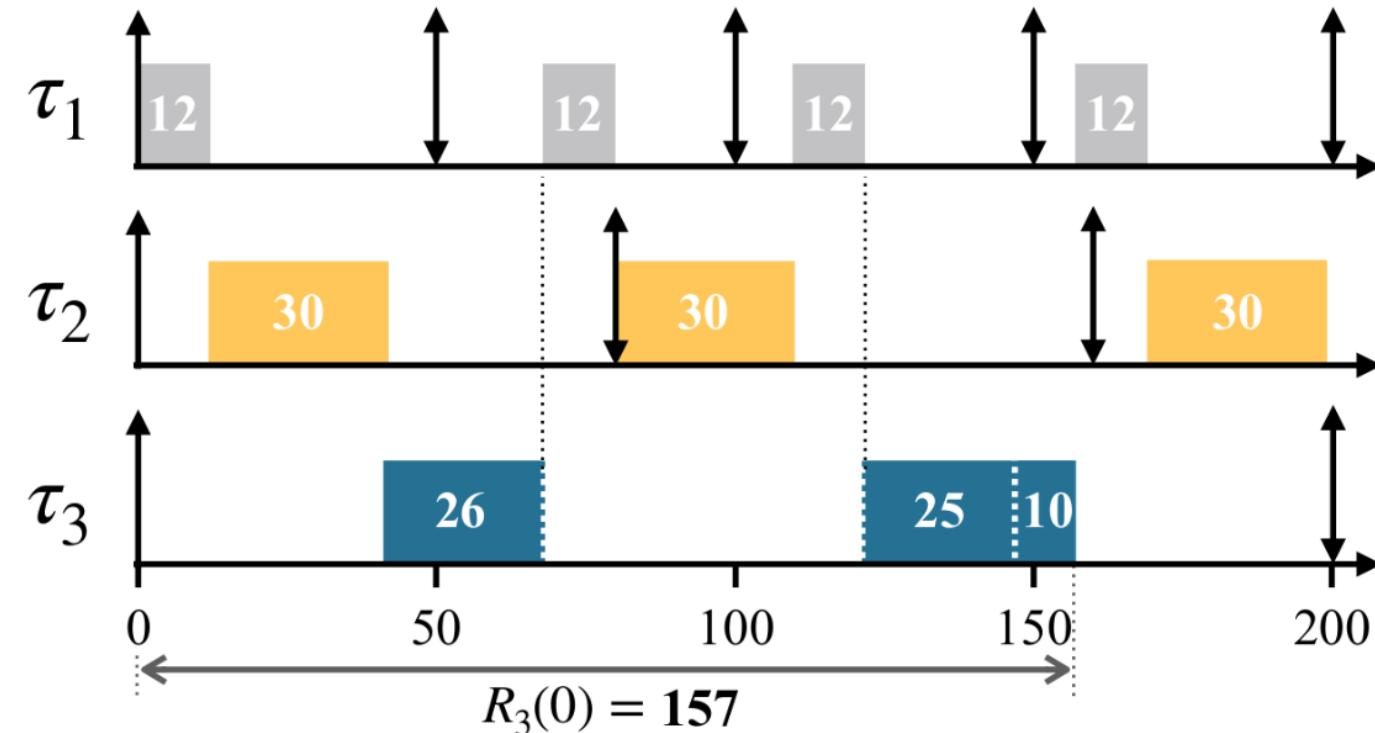
- Honestly, I still don't have a strong opinion ☺
  - A measure of uncertainty in  $[0, 1]$  for each execution time bound?
- **Pragmatic observations:**
  - Execution time estimates can be obtained by **measurements** (*nominal exec. times*)
  - Code **complexity** affects uncertainty
    - More branching  $\rightarrow$  more uncertainty (e.g., consider branch prediction)
    - More paths  $\rightarrow$  unpredictable cache hit/miss patterns  $\rightarrow$  more uncertainty
  - **Memory access** affects uncertainty
    - More memory accesses  $\rightarrow$  more opportunity for contention  $\rightarrow$  more uncertainty
  - **Coverage** affects uncertainty
    - Less coverage during measurements  $\rightarrow$  more uncertainty

# Motivating Example

From Matteo Zini's presentation @ RTSS 2024

For example, consider this simple limited-preemptive taskset:

Task	Period	NET
$\tau_1$	50	<12>
$\tau_2$	80	<30>
$\tau_3$	200	<26,25,10>



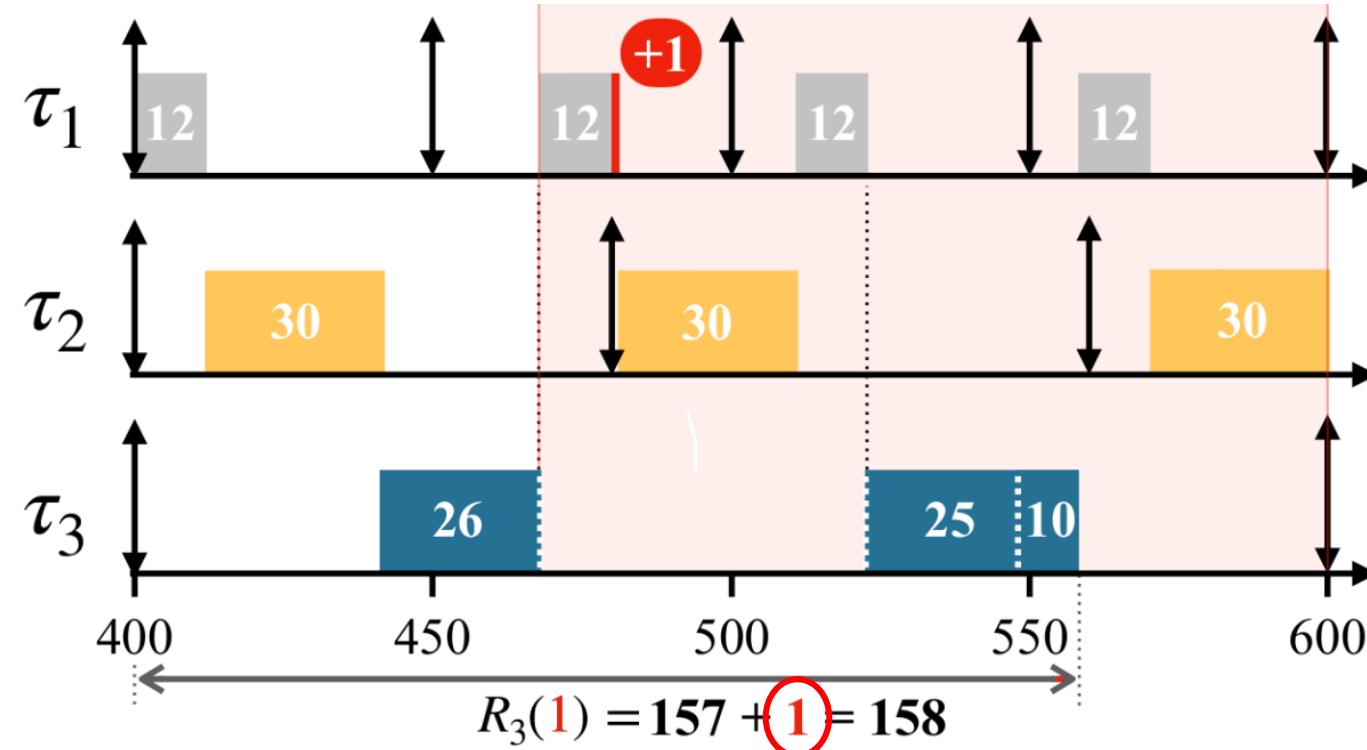
# Motivating Example

From Matteo Zini's presentation @ RTSS 2024

We add 1 unit of exceedance to the second job of task  $\tau_1$



Task	Period	NET
$\tau_1$	50	<12>
$\tau_2$	80	<30>
$\tau_3$	200	<26,25,10>



$\tau_3$ 's response time increased by 1 time unit

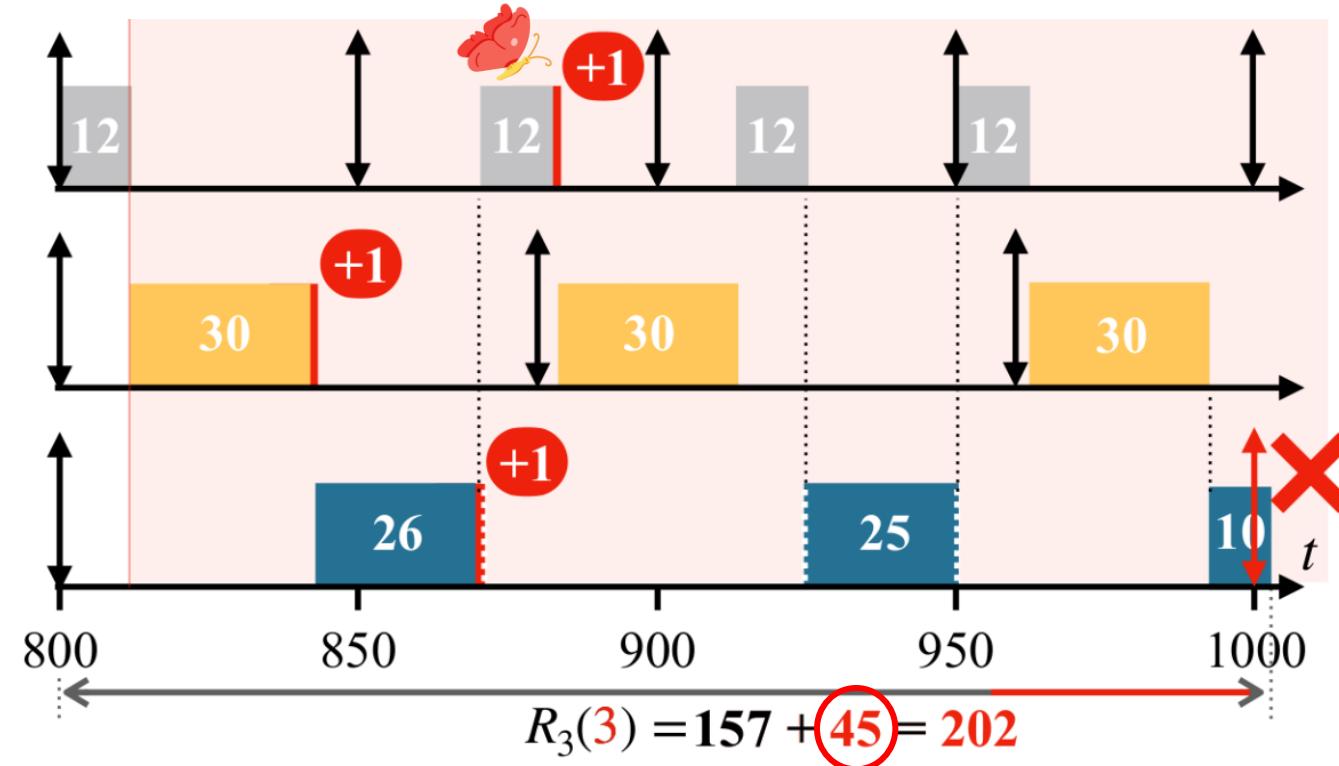
# Motivating Example

From Matteo Zini's presentation @ RTSS 2024

We add 1 unit of exceedance to the first job of task  $\tau_2$  and  $\tau_3$




Task	Period	NET
$\tau_1$	50	<12>
$\tau_2$	80	<30>
$\tau_3$	200	<26,25,10>



$\tau_3$ 's response time increased by 45 time units!

# Response-Time Nonlinearities

From Matteo Zini's presentation @ RTSS 2024

The consequences of **NET exceedance** are not easy to predict:

- NET + 1  $\longrightarrow$  Response time + 1
- NET + 2  $\longrightarrow$  Response time + 2
- NET + 3  $\longrightarrow$  Response time **+ 45**  $\longrightarrow$  **Nonlinear increase!**
- ...

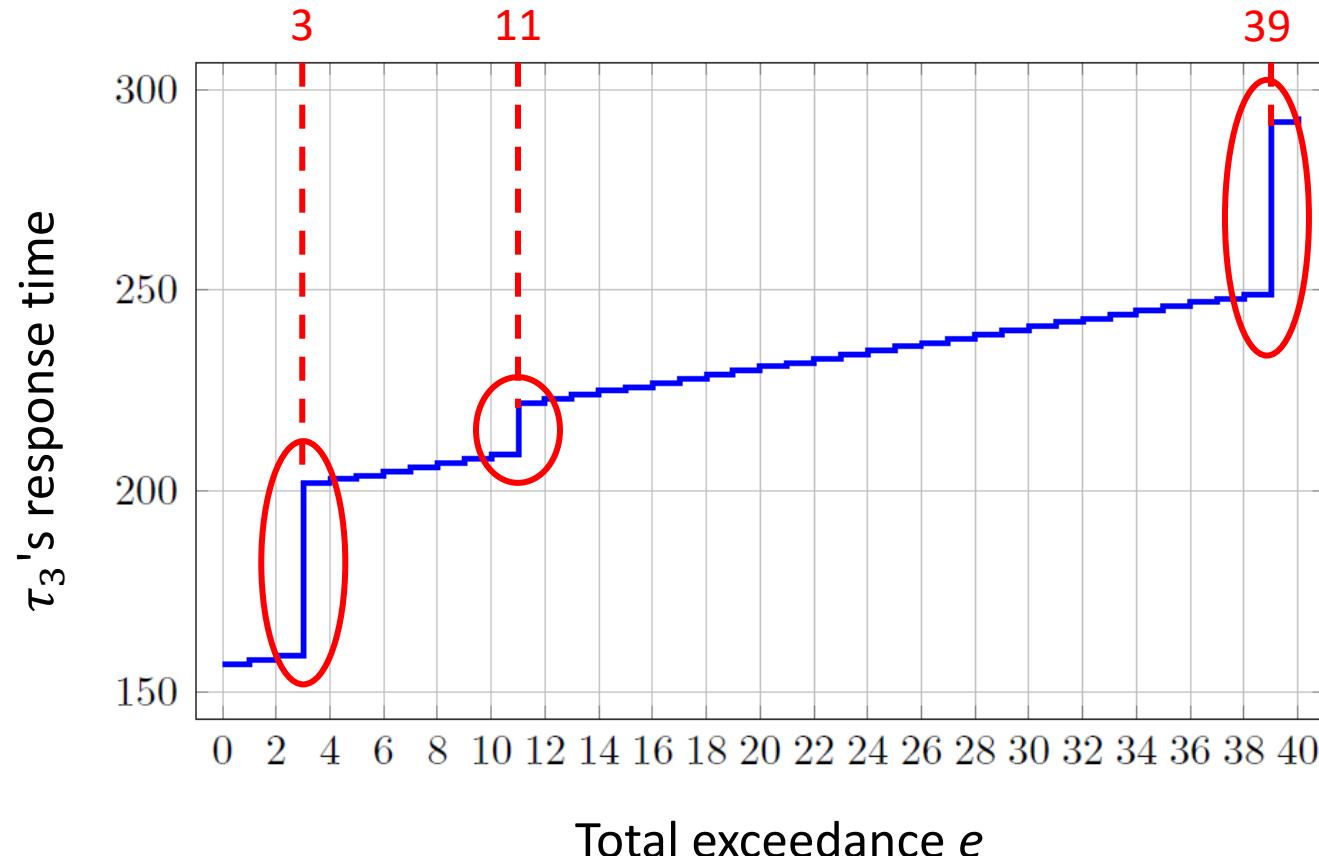
If we neglect this phenomenon, we might **over-estimate the system's temporal safety margin**

# Response-Time Discontinuities

From Matteo Zini's presentation @ RTSS 2024

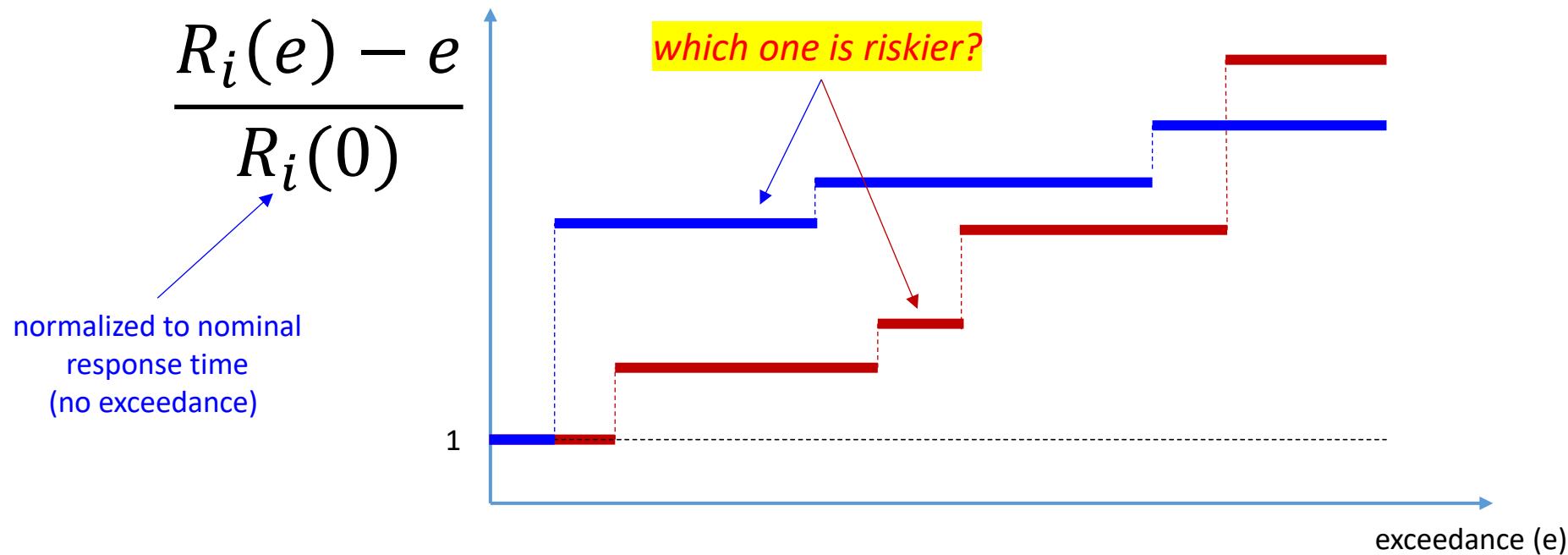
Response-time discontinuities are not trivial to predict

Task	Period	NET
$\tau_1$	50	<12>
$\tau_2$	80	<10, 20>
$\tau_3$	200	<26,25,10>



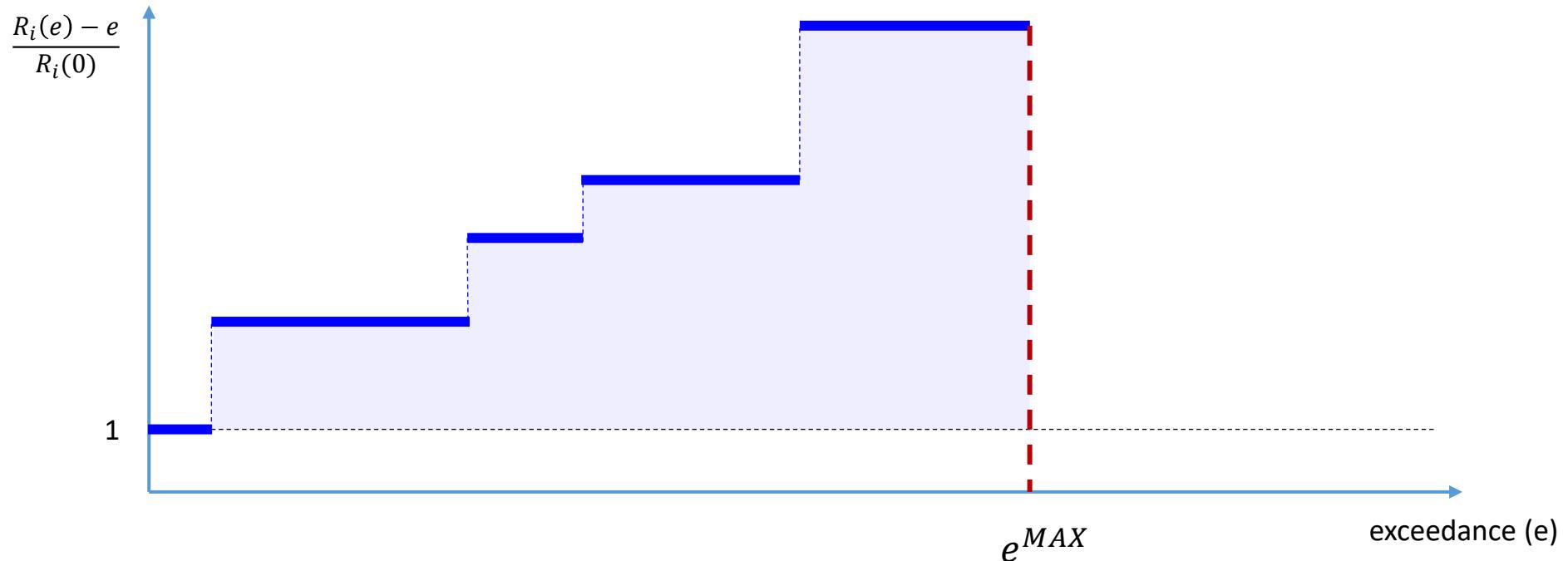
# Risk Factor

- When a system experiences **exceedance**, the **best** it can happen is a **linear, unitary-slope increase** in response times
  - Risk** is determined by **discontinuous increases** of response times (jumps)
  - Hence  $R_i(e) - e$  determines risk



# Risk Factor

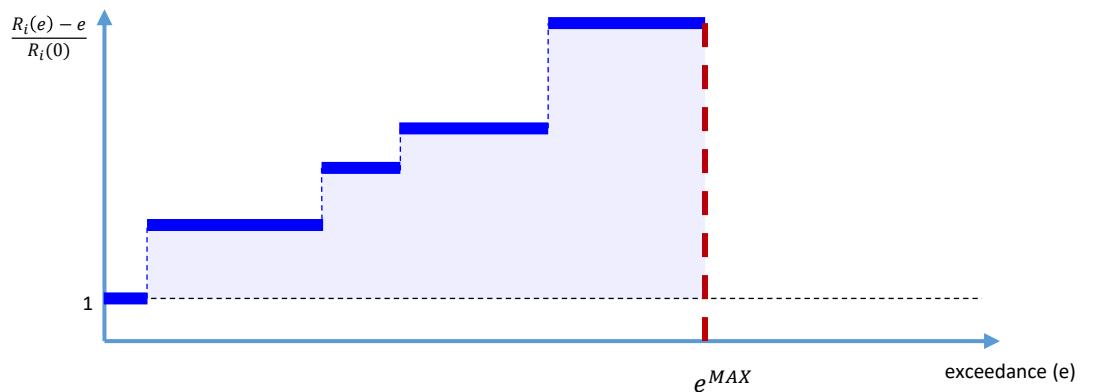
$$\gamma_i(e^{MAX}) = \int_0^{e^{MAX}} \frac{R_i(e) - e}{R_i(0)} - 1 \ de$$



# Risk Factor

- **Informal interpretation of risk factor  $\gamma_i(e^{MAX})$** 
  - It captures “*how much*” exceedance introduces large discontinuous increases
  - It captures “*how quickly*” response times jump with exceedance
- This definition depends on the maximum expected exceedance  $e^{MAX}$ 
  - Ouch...yet another parameter?

$$\gamma_i(e^{MAX}) = \int_0^{e^{MAX}} \frac{R_i(e) - e}{R_i(0)} - 1 \ de$$



# Minimizing Risk Factor

- **Challenge:** *Design real-time systems to minimize risk factor*
  - Either for a selection of tasks or all tasks
  - Weighting risk factor by a trustworthiness/uncertainty level of execution times
  - Considering arbitrary maximum expected exceedance
- **It's an optimization problem**

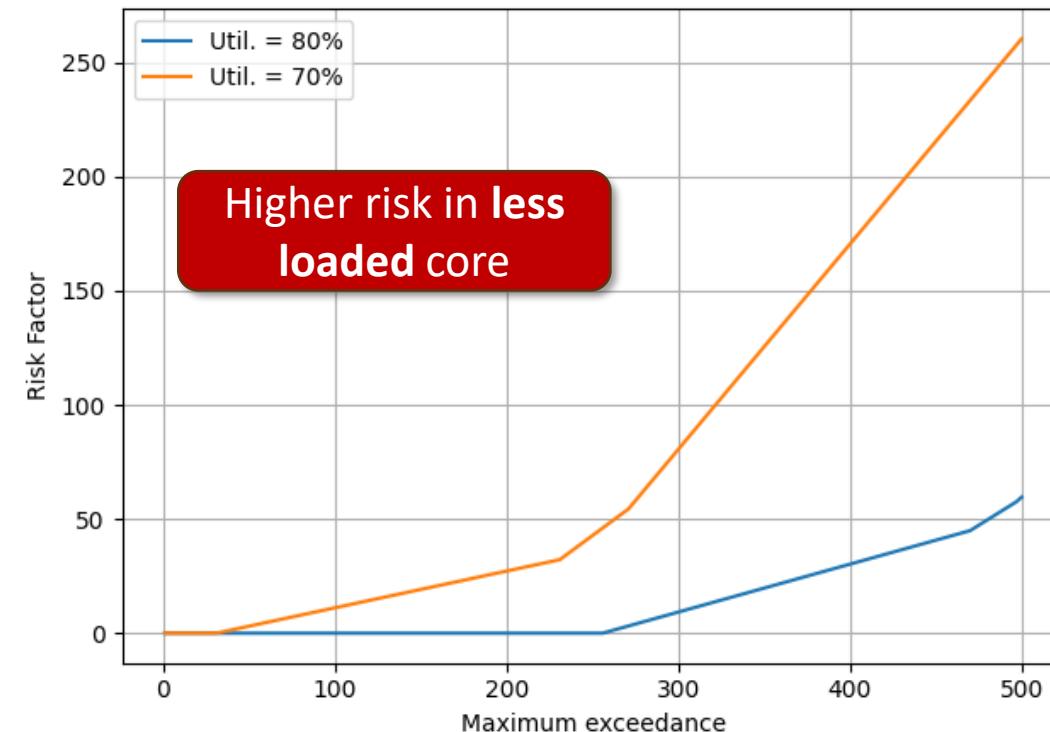
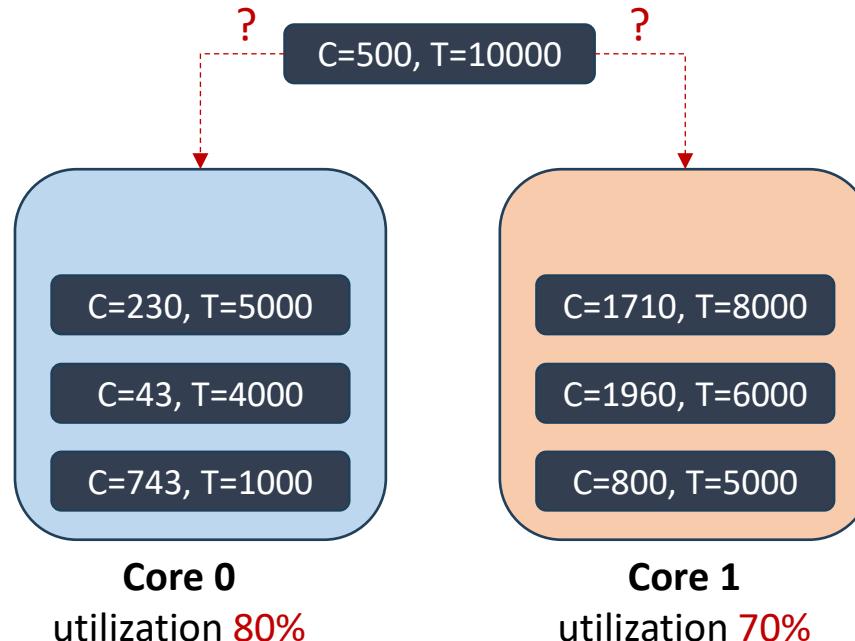
## Examples:

- Partition tasks on multicores according to risk
- Find task periods that minimize risk while securing control performance
- Configure locking protocols to minimize risk
- Configure Logical Execution Time (LET) intervals according to risk
- ...

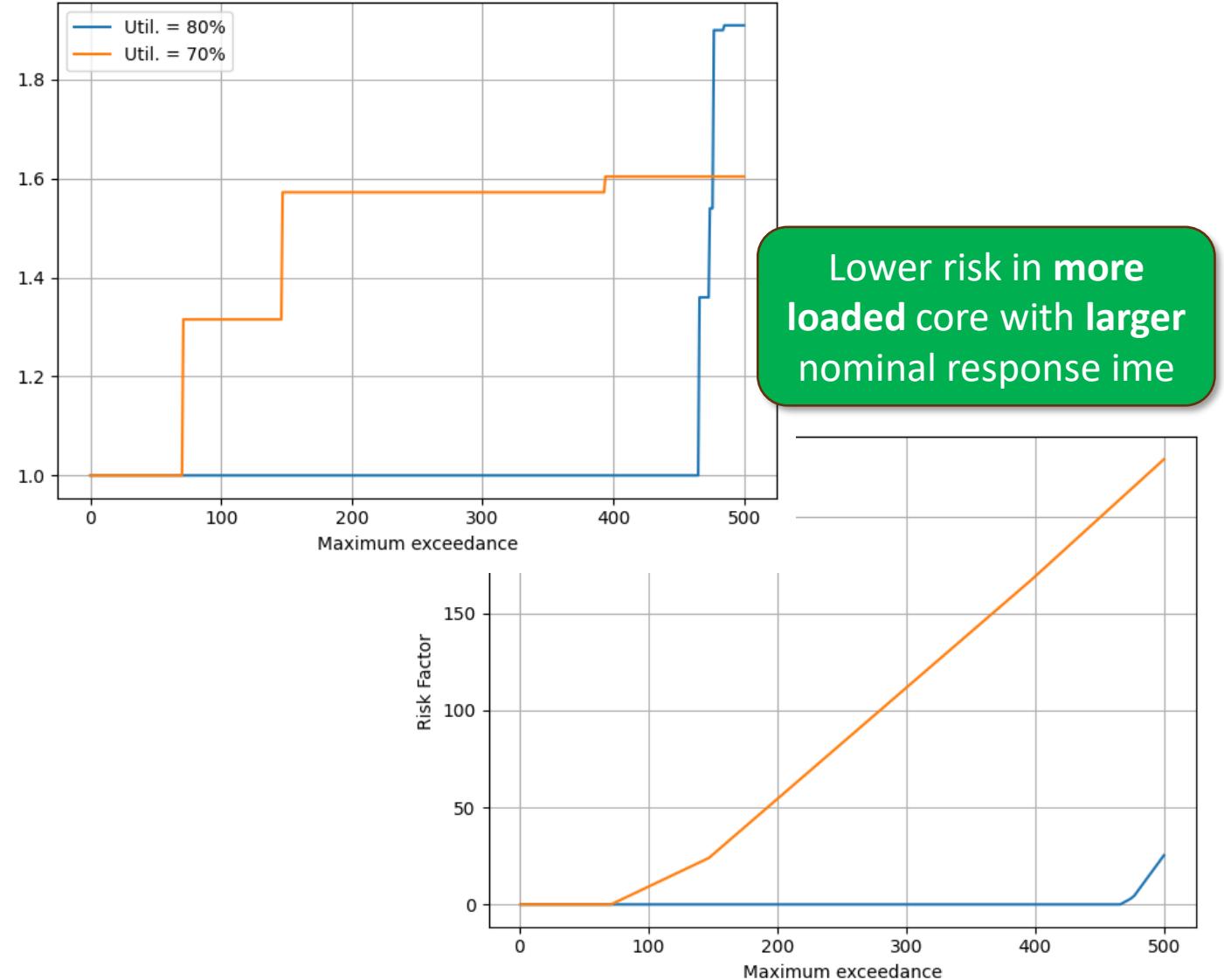
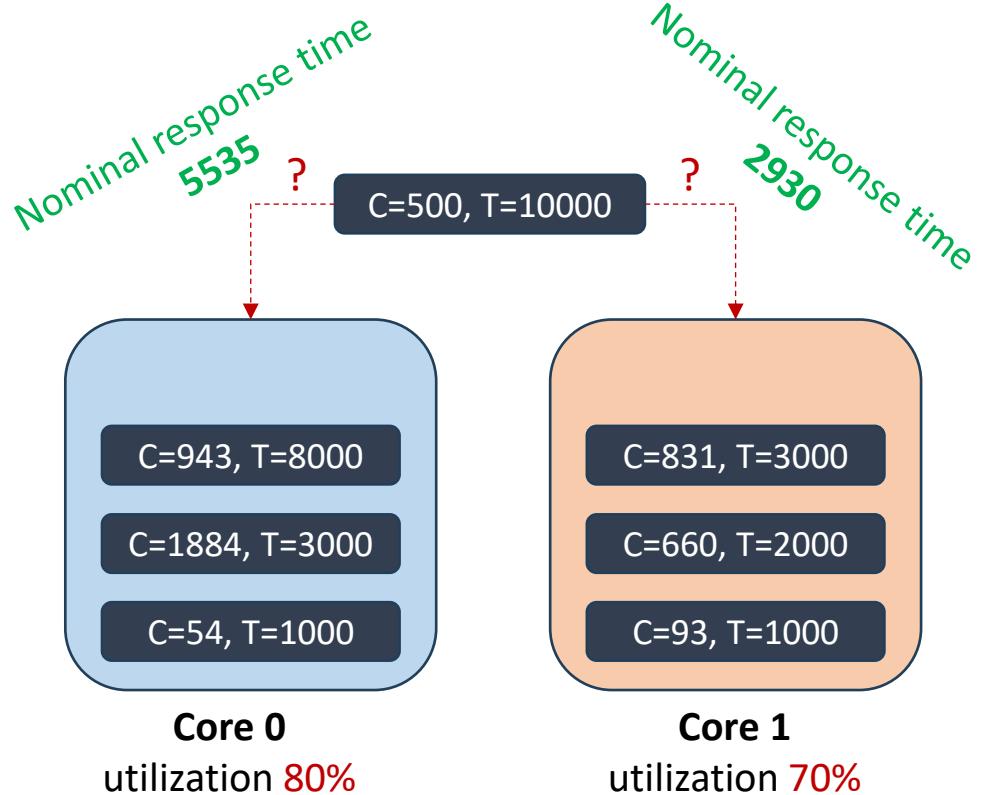
Subject to classical schedulability under **nominal execution times**

# Example: Task Partitioning (1)

- Place tasks to cores to minimize risk factor
  - E.g., for a target, relevant task
- Partitioned fixed-priority scheduling of Liu&Layland tasks**
  - Even with a simple scheduler and task model, decisions are not obvious



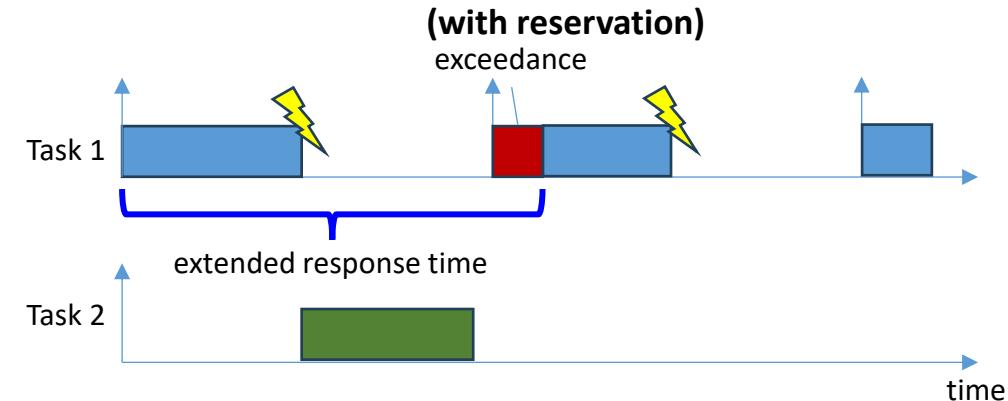
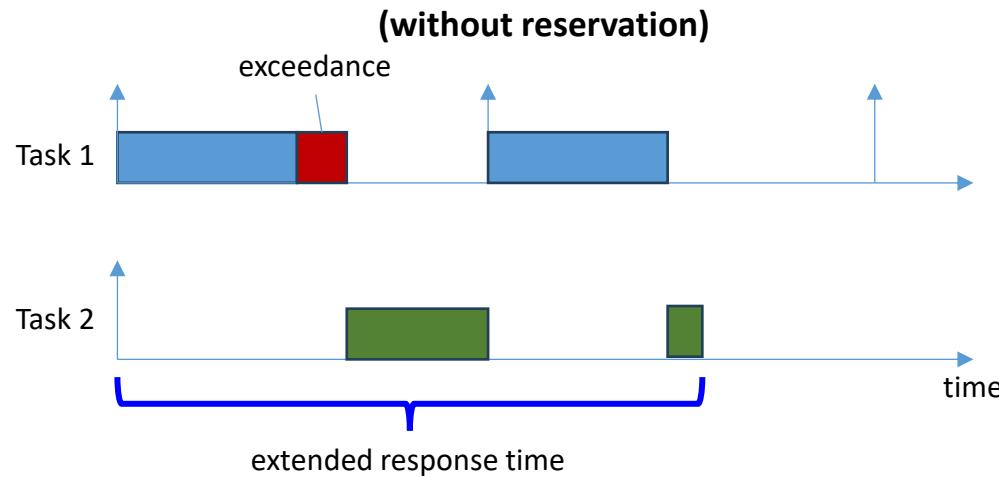
# Example: Task Partitioning (2)



# Achieving Resiliency

- **Reservation servers** work great to isolate the effects of exceedance
  - It's a way to control uncertainty

Since late 90's



- Can we design an **adaptive** reservation mechanism that **minimizes the risk factor**?
  - **Budget reclaiming** is very effective (since early 2000's)

There's space for new reservation algorithms that, jointly applied with budget reclaiming, limit response-time discontinuities and hence the risk factor

# Thank you!

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